

THE DEPARTMENT OF MATHEMATICAL SCIENCES

MATH 337: Linear Algebra

Fall 2024 Course Syllabus

NJIT Academic Integrity Code: All Students should be aware that the Department of Mathematical Sciences takes the University Code on Academic Integrity at NJIT very seriously and enforces it strictly. This means that there must not be any forms of plagiarism, i.e., copying of homework, class projects, or lab assignments, or any form of cheating in quizzes and exams. Under the University Code on Academic Integrity, students are obligated to report any such activities to the Instructor.

COURSE INFORMATION

Course Description: Matrices, determinants, systems of linear equations, vector spaces, linear transformations, eigenvalues, eigenvectors, and related topics.

Number of Credits: 3

Prerequisites: MATH 112 with a grade of C or better or MATH 133 with a grade of C or better.

Course-Section and Instructors:

| Course-Section | Instructor |
|----------------|------------------------|
| Math 337-001 | Professor J. Luke |
| Math 337-003 | Professor R. Goodman |
| Math 337-005 | Professor J. Luke |
| Math 337-007 | Professor T. P. Nguyen |
| Math 337-101 | Professor E. Ammicht |

Office Hours for All Math Instructors: Fall 2024 Office Hours and Emails

Required Textbook:

| | |
|-----------|---|
| Title | <i>A First Course in Linear Algebra</i> |
| Author | K. Kuttler and I. Farah |
| Edition | Version 2021 A |
| Publisher | Lyryx Learning Inc |
| Link | Available in Canvas |

University-wide Withdrawal Date: The last day to withdraw with a W is **Monday, November 11, 2024**. It will be strictly enforced.

COURSE GOALS

Course Objectives:

The course seeks to develop

- understanding of the fundamental concepts of linear structure that support theoretical, applied and computational analysis primarily in \mathbb{R}^n but also in \mathbb{C}^n . These concepts include formation of linear combinations, span, linear independence, basis and dimension, Euclidean structure, matrices and linear transformations, invertibility, rank, fundamental subspaces, and determinant,
- understanding of the fundamental algorithms of elementary linear algebra, notably Gauss-Jordan elimination and the Gram-Schmidt process, including proficiency in implementation both with pen and paper and by computer program,
- the ability to use linear theory, including spectral theory, to analyze problems common in applications including systems of linear equations, detection linear dependence relations, LU factorization, diagonalization, orthogonalization, QR factorization, least squares solutions, and the singular value decomposition,
- basic proficiency, both with pen and paper and by computer program, with the use of the fundamental algorithms of elementary linear algebra for the solution of common problems including those listed above,
- mastery of the basic elements of two fundamental problems of linear algebra, solving linear systems and diagonalizing matrices, from both a theoretical and computational perspective.
- the capacity to apply linear algebra through treatment of applications such as balancing chemical equations and computer graphics.

Course Outcomes:

Students will be able to

- understand and utilize the basic concepts and methods of linear algebra to analyze basic applied problems,
- solve linear equations of equations and find eigenvalues and eigenvectors to enable diagonalization,
- implement basic solutions to problems of applied linear algebra both by hand and computer program (MATLAB),
- apply their understanding of linear algebra in appropriately formulated applications.

POLICIES

DMS Course Policies: All DMS students must familiarize themselves with, and adhere to, the **Department of Mathematical Sciences Course Policies**, in addition to official **university-wide policies**. DMS takes these policies very seriously and enforces them strictly.

Grading Policy: The final grade in this course will be determined as follows:

| | |
|-----------------------|----------|
| Quizzes | 15% |
| MATLAB Assignments | 15% |
| Midterm Exams | 20% (x2) |
| Final Cumulative Exam | 30% |

Your final letter grade will be based on the following tentative curve.

| | | | |
|----|----------|---|---------|
| A | 90 - 100 | C | 70 - 74 |
| B+ | 85 - 89 | D | 60 - 69 |
| B | 80 - 84 | F | 0 - 59 |
| C+ | 75 - 79 | | |

Attendance Policy: Attendance at all classes will be recorded and is **mandatory**. Please make sure you read and fully understand the **Math Department's Attendance Policy**. This policy will be strictly enforced.

Common Quizzes: Online quizzes, given on a roughly weekly basis, will focus on a collection of fifteen fundamental computations that are foundational for the course. The intention of the quizzes is to provide students an opportunity to begin mastery of these crucial computations on which much of the course depends. Instructors may supplement the common quizzes with quizzes specifically for their sections.

MATLAB Projects: Weekly MATLAB projects will cover the implementation and use of basic algorithms in linear algebra. The coding of the algorithms is not only a tool of application but also a pathway for understanding. Common exams will feature problems requiring proficiency with MATLAB implementation of basic algorithms.

Homework: Homework assignments are provided to assist students to develop their understanding and skills with linear algebra. These assignments are neither collected or graded. Students should develop and use judgment as to which exercises are needed for them to develop adequate understanding of the material. The standing advice, particularly at the beginning of the course, is that it is better to do too much than too little. Students are urged to seek assistance with problems and exercises with which they have struggled unsuccessfully.

Exams: There will be two exams during the semester and a cumulative final exam during the final exam week:

| | |
|-------------------|----------------------------------|
| Midterm Exam I | October 9, 2024 |
| Midterm Exam II | November 13, 2024 |
| Final Exam Period | December 15 to December 21, 2024 |

The final exam will test your knowledge of all the course material taught in the entire course. Make sure you read and fully understand the **Math Department's Examination Policy**. This policy will be strictly enforced.

Makeup Exam Policy: There will be **NO MAKE-UP QUIZZES OR EXAMS** during the semester. In the event an exam is not taken under rare circumstances where the student has a legitimate reason for missing the exam, the student should contact the Dean of Students office and present written verifiable proof of the reason for missing the exam, e.g., a doctor's note, police report, court notice, etc. clearly stating the date AND time of the mitigating problem. The student must also notify the Math Department Office/Instructor that the exam will be missed.

Cellular Phones: All cellular phones and other electronic devices must be switched off during all class times.

ADDITIONAL RESOURCES

Math Tutoring Center: Located in the Central King Building, Lower Level, Rm. G11 (See: **Fall 2024 Hours**)

Further Assistance: For further questions, students should contact their instructor. All instructors have regular office hours during the week. These office hours are listed on the Math Department's webpage for [Instructor Office Hours and Emails](#).

Accommodation of Disabilities: The Office of Accessibility Resources and Services (OARS) offers long term and temporary accommodations for undergraduate, graduate and visiting students at NJIT.

If you need an accommodation due to a disability, please contact the Office of Accessibility Resources and Services at oars@njit.edu, or visit Kupfrian Hall 201 to discuss your specific needs. A Letter of Accommodation Eligibility from the office authorizing student accommodations is required.

For further information regarding self identification, the submission of medical documentation and additional support services provided please visit the Office of Accessibility Resources and Services (OARS) website at:

<https://www.njit.edu/accessibility/>

Important Dates (See: [Fall 2024 Academic Calendar, Registrar](#))

| Date | Day | Event |
|----------------------------------|---------------------|------------------------------|
| September 2, 2024 | Monday | Labor Day |
| September 3, 2024 | Tuesday | First Day of Classes |
| September 9, 2024 | Monday | Last Day to Add/Drop Classes |
| November 11, 2024 | Monday | Last Day to Withdraw |
| November 26, 2024 | Tuesday | Thursday Classes Meet |
| November 27, 2024 | Wednesday | Friday Classes Meet |
| November 28 to December 1, 2024 | Thursday and Sunday | Thanksgiving Recess - Closed |
| December 11, 2024 | Wednesday | Last Day of Classes |
| December 12, 2024 | Thursday | Reading Day 1 |
| December 13, 2024 | Friday | Reading Day 2 |
| December 15 to December 21, 2024 | Sunday to Saturday | Final Exam Period |

Course Outline

The lecture schedule is suggested only and will vary depending on the section instructor's discretion.

| Meeting | Lesson | Topics |
|---------|--------|--|
| 1 | I.1 | Vectors, Linear Combinations, Lengths and Angles |

| | | |
|----|-------|---|
| 2 | I.2 | Small Linear Systems |
| 3 | I.3 | The Gauss-Jordan Elimination Algorithm: Preliminaries |
| 4 | I.4 | The Gauss-Jordan Elimination Algorithm: Implementation |
| 5 | I.5 | Parametric Vector Form |
| 6 | I.6 | Vectors and Matrices |
| 7 | I.7 | Matrix Inverse |
| 8 | I.8 | Matrix Factorization with Elementary Matrices |
| 9 | I.9 | Linear Transformations |
| 10 | | Review for Common Exam I |
| 11 | II.1 | Families of Matrices |
| 12 | II.2 | Determinants |
| 13 | II.3 | Characteristic Polynomials, Eigenvalues and Diagonalization of 2x2 Matrices |
| 14 | II.4 | Euclidean Vector Spaces |
| 15 | II.5 | Spanning, Independence, Basis and Dimension |
| 16 | II.6 | The Four Fundamental Subspaces |
| 17 | II.7 | Diagonalization of Small Matrices |
| 18 | II.8 | Orthogonalization, Least Squares and Regression |
| 19 | | Review for Common Exam II |
| 20 | III.1 | The Gram-Schmidt Orthonormalization Process and the QR Factorization |
| 21 | III.2 | Diagonalization of nxn Matrices |
| 22 | III.3 | Linear Difference Equations and Markov Chains |
| 23 | III.4 | IVP for Linear Systems of ODES |
| 24 | III.5 | Rotations and Their Logarithms |
| 25 | III.6 | Orthogonal Diagonalization |
| 26 | III.7 | SVD I |
| 27 | III.8 | SVD II |
| 28 | | Review for the Final Exam |

*Updated by Professor J. Luke -
Department of Mathematical Sciences Course Syllabus, Fall 2024*